



# Split Learning

A resource efficient distributed deep learning method without sensitive data sharing

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'Invisible' Health Image Data







'Small Data'



'Small Data'







## ML for Health Images



- a. Distributed Data
- b. Patient privacy
- c. Incentives
- d. ML Expertise
- e. Efficiency













Gupta, Raskar 'Distributed training of deep neural network over several agents', 2017

## Intelligent Computing

**Top Perceived Advantages of Using AI for Health Care** 

### Security, Privacy & Safety

## ... and predictive models can breach privacy too



## Regulations

**GDPR:** General Data Protection Regulation **HIPAA:** Health Insurance Portability and Accountability Act, 1996 **SOX**: Sarbanes-Oxley Act, 2002 **PCI**: Payment Card Industry Data Security Standard, 2004 **SHIELD:** Stop Hacks and Improve Electronic Data Security Act, Jan 1 2019

## **NOTABLE HEALTHCARE BREACHES**





## **Challenges for Distributed Data + AI + Health**

Distributed Data Multi-Modal Incomplete Data

Ledgering Smart contracts Maintenance Regulations Incentives Cooperation Ease

Resource-constraints Memory, Compute, Bandwidth, Convergence, Synchronization, Leakage

## Automating ML : Al building Al



Otkrist Gupta, Baker, Naik, Raskar, ICLR 2017

AI: Bringing it all together

Training Deep Networks

## No sharing of Raw Images

Server

Client

Invisible Data / Data Friction

**Overcoming Data Friction** 

# Ease Incentive Trust Regulation

Blockchain

AI/ SplitNN

## Anonymize Obfuscate

## Encrypt

**Protect Data** 

## Anonymity is not enough ...

#### A Face Is Exposed for AOL Searcher No. 4417749

By MICHAEL BARBARO and TOM ZELLER Jr. Published: August 9, 2006





#### Why 'Anonymous' Data Sometimes Isn't

By Bruce Schneier 🖂 12.13.07

Last year, Netflix published 10 million movie rankings by 500,000 customers, as part of a challenge for people to come up with better recommendation systems than the one the company was using.

SIGN IN TO E

The Scientist » The Nutshell

#### "Anonymous" Genomes Identified

The names and addresses of people participating in the Personal Genome Project can be easily tracked down despite such data being left off their online profiles.

By Dan Cossins | May 3, 2013





Federated Learning Nets trained at Clients Merged at Server

Differential Privacy Obfuscate with noise Hide unique samples Split Learning (MIT) Nets split over network Trained at both

Homomorphic Encryption Basic Math over Encrypted Data (+, x)



Protect data Distributed Training	Partial Leakage	Differential Privacy	Homomorphic Encryption	Oblivious Transfer, Garbled Circuits
Federated Learning		<u> </u>	<u> </u>	<u> </u>
Split Learning				

Inference but no training

Praneeth Vepakomma, Tristan Swedish, Otkrist Gupta, Abhi Dubey, Raskar 2018

## When to use split learning?



<u>Large number of clients:</u> Split learning shows positive results

Memory Compute Bandwidth Convergence

Project Page and Papers: https://splitlearning.github.io/

## QUANTITATIVE RESULTS

Method	100 Clients	500 Clients				
Large Scale SGD	29.4 TFlops	5.89 TFlops				
Federated Learning	29.4 TFlops	5.89 TFlops				
Our Method (SplitNN)	0.1548 TFlops	0.03 TFlops				
Table 1. Computation resources consumed per client when training CIFAR 10 over VGG (in teraflops)						
Method	100 Clients	500 Clients				
Large Scale SGD	13 GB	14 GB				
Federated Learning	3 GB	2.4 GB				
Our Method (SplitNN)	6 GB	1.2 GB				
Table 2. Communication Bandwidth consumed per client when training CIFAR 100 and Resnet 50 (in gigabytes)						





No Label Sharing





Gupta, Otkrist, and Raskar, Ramesh. "Secure Training of Multi-Party Deep Neural Network." U.S. Patent Application No. 15/630,944.

## Distribution of parameters in AlexNet

Layer Name	Tensor Size	Weights	Biases	Parameters
Input Image	227x227x3	0	0	0
Conv-1	55x55x96	34,848	96	34,944
MaxPool-1	27x27x96	0	0	0
Conv-2	27x27x256	614,400	256	614,656
MaxPool-2	13x13x256	0	0	0
Conv-3	13x13x384	884,736	384	885,120
Conv-4	13x13x384	1,327,104	384	1,327,488
Conv-5	13x13x256	884,736	256	884,992
MaxPool-3	6x6x256	0	0	0
FC-1	4096×1	37,748,736	4,096	37,752,832
FC-2	4096×1	16,777,216	4,096	16,781,312
FC-3	1000×1	4,096,000	1,000	4,097,000
Output	1000×1	0	0	0
Total				62,378,344

## Versatile Configurations of Split Learning



Split learning for health: Distributed deep learning without sharing raw patient data, Praneeth Vepakomma, Otkrist Gupta, Tristan Swedish, Ramesh Raskar, (2019)

## NoPeek SplitNN: Reducing Leakage in Distributed Deep Learning



$$\alpha_1 DCOR(\mathbf{X_n}, \mathbf{\hat{Z}}) + \alpha_2 CCE(\mathbf{\hat{Y}}, \mathbf{Y_n})$$

Reducing leakage in distributed deep learning for sensitive health data, Praneeth Vepakomma, Otkrist Gupta, Abhimanyu Dubey, Ramesh Raskar (2019)

No peak deep learning with conditioning variable

Setup:

- Supervised:  $D = \{(\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \dots, (\mathbf{x}_m, y_m)\} \subset X \times Y$
- Output:  $y \in \mathbb{R}$
- Goal : To find a projection  $S_{Y|X}$  such that,  $Y \perp \!\!\!\perp X|Z$ .

**Ideal Goal:** To find such a conditioning variable Z <u>within the framework of deep learning</u> such that the following directions are approximately satisfied:

- 1. Y  $\perp \perp$  X | Z (Utility property as X can be thrown away given Z to obtain prediction E(Y|Z))
- 2. X <u>||</u> Z (One-way property preventing proper reconstruction of raw data X from Z)

*Note:* <u>||</u> *denotes statistical independence* 

## Possible measures of non-linear dependence

- COCO: Constrained Covariance
- HSIC: Hilbert-Schmidt Independence Criterion
- DCOR: Distance Correlation
- MMD: Maximum Mean Discrepancy
- KTA: Kernel Target Alignment
- MIC: Maximal Information Coefficient
- TIC: Total Information Coefficient

### Why is it called distance correlation?

**Definition 3.1. Sample Distance Covariance [3]:** Given i.i.d samples  $\mathcal{X} \times \mathcal{Y} = \{(\mathbf{x}_k, \mathbf{y}_k) | k = 1, 2, 3, ..., n\}$  and corresponding double centered Euclidean distance matrices  $\widehat{\mathbf{E}}_{\mathbf{X}}$  and  $\widehat{\mathbf{E}}_{\mathbf{Y}}$ , then the squared sample distance correlation is defined as,



Distance Covariance (Székely, G. (2007))

$$\nu^{2}(\mathbf{X},\mathbf{Y};w) = \int_{\mathbb{R}^{h+m}} |f_{\mathbf{X},\mathbf{Y}}(t,s) - f_{\mathbf{X}}(t)f_{\mathbf{Y}}(s)|^{2}w(t,s)dtds$$

where  $f_{\mathbf{X}}, f_{\mathbf{Y}}, f_{\mathbf{X},\mathbf{Y}}$  are the characteristic functions of  $\mathbf{X}, \mathbf{Y}, \mathbf{X} \times \mathbf{Y}$  and w(t, s) is a suitably chosen weight function.



**Lemma 3.1.** Given matrices of squared Euclidean distances  $\mathbf{E}_{\mathbf{X}}$  and  $\mathbf{E}_{\mathbf{Y}}$  and Laplacians  $\mathbf{L}_{\mathbf{X}}$  and  $\mathbf{L}_{\mathbf{Y}}$  formed over adjacency matrics  $\widehat{\mathbf{E}}_{\mathbf{X}}$  and  $\widehat{\mathbf{E}}_{\mathbf{Y}}$ , the square of sample distance correlation  $\hat{\rho}^2(\mathbf{X}, \mathbf{Y})$  is given by

$$\hat{\rho}^2(\mathbf{X}, \mathbf{Y}) = \frac{\operatorname{Tr} \left( \mathbf{X}^T \mathbf{L}_{\mathbf{Y}} \mathbf{X} \right)}{\sqrt{\operatorname{Tr} \left( \mathbf{Y}^T \mathbf{L}_{\mathbf{Y}} \mathbf{Y} \right) \operatorname{Tr} \left( \mathbf{X}^T \mathbf{L}_{\mathbf{X}} \mathbf{X} \right)}}.$$

Praneeth Vepakomma, Chetan Tonde, Ahmed Elgammal, Electronic Journal of Statistics, 2018

## Colorectal histology image dataset (Public data)



## Leakage Reduction in Action



Reduced leakage during training over colorectal histology image data from 0.96 in traditional CNN to 0.19 in NoPeek SplitNN



Reduced leakage during training over colorectal histology image data from 0.92 in traditional CNN to 0.33 in NoPeek SplitNN

Reducing leakage in distributed deep learning for sensitive health data, Praneeth Vepakomma, Otkrist Gupta, Abhimanyu Dubey, Ramesh Raskar (2019)

## Similar validation performance





## Effect of leakage reduction on convergence



### Robustness to reconstruction



## Proof of one-Way Property:

$$DCOV(\mathbf{X}, \mathbf{Z}) = Tr(\mathbf{X}\mathbf{X}^{T}\mathbf{Z}\mathbf{Z}^{T}) + \|\mathbf{X} - \mathbf{Z}\| + \|\mathbf{Z}\|$$

$$D_{KL}(\mathbf{Z}||\mathbf{X}) - D_{KL}(\mathbf{X}||\mathbf{Z}) = H(\mathbf{Z}, \mathbf{X}) - H(\mathbf{Z}) - H(\mathbf{X}, \mathbf{Z}) + H(\mathbf{X})$$

We show: Minimizing regularized distance covariance minimizes the difference of Kullback-Leibler divergences

$$= \det(\mathbf{Z}^{\mathbf{T}}\mathbf{X}) - \det(\mathbf{Z}^{\mathbf{T}}\mathbf{Z}) - \det(\mathbf{X}^{\mathbf{T}}\mathbf{Z}) + \det(\mathbf{X}^{\mathbf{T}}\mathbf{X})$$

This can be bounded using Hadamard's inequality as

$$\begin{aligned} \det(\mathbf{Z}^{\mathsf{T}}\mathbf{X}) &- \det(\mathbf{Z}^{\mathsf{T}}\mathbf{Z}) + \det(\mathbf{X}^{\mathsf{T}}\mathbf{X}) - \det(\mathbf{X}^{\mathsf{T}}\mathbf{Z}) \leq \left\|\mathbf{Z}^{\mathsf{T}}\mathbf{X} - \mathbf{Z}^{\mathsf{T}}\mathbf{Z}\right\|_{2} \frac{\left\|\mathbf{Z}^{\mathsf{T}}\mathbf{X}\right\|_{2}^{n} - \left\|\mathbf{Z}^{\mathsf{T}}\mathbf{Z}\right\|_{2}^{n}}{\left\|\mathbf{Z}^{\mathsf{T}}\mathbf{X}\right\|_{2} - \left\|\mathbf{Z}^{\mathsf{T}}\mathbf{Z}\right\|_{2}} \\ &+ \left\|\mathbf{X}^{\mathsf{T}}\mathbf{Z} - \mathbf{X}^{\mathsf{T}}\mathbf{X}\right\|_{2} \frac{\left\|\mathbf{X}^{\mathsf{T}}\mathbf{Z}\right\|_{2}^{n} - \left\|\mathbf{X}^{\mathsf{T}}\mathbf{X}\right\|_{2}^{n}}{\left\|\mathbf{X}^{\mathsf{T}}\mathbf{Z}\right\|_{2}^{n} - \left\|\mathbf{X}^{\mathsf{T}}\mathbf{X}\right\|_{2}} \end{aligned}$$

The fractional terms  $\frac{\|\mathbf{Z}^{T}\mathbf{X}\|_{2}^{n} - \|\mathbf{Z}^{T}\mathbf{X}\|_{2}^{n}}{\|\mathbf{Z}^{T}\mathbf{X}\|_{2} - \|\mathbf{Z}^{T}\mathbf{Z}\|_{2}}, \quad \frac{\|\mathbf{X}^{T}\mathbf{Z}\|_{2}^{n} - \|\mathbf{X}^{T}\mathbf{X}\|_{2}^{n}}{\|\mathbf{X}^{T}\mathbf{Z}\|_{2} - \|\mathbf{X}^{T}\mathbf{X}\|_{2}} \text{ can be written as a sum of geometric-series, with factors of change of } \frac{\|\mathbf{Z}^{T}\mathbf{X}\|}{\|\mathbf{X}^{T}\mathbf{Z}\|}, \quad \frac{\|\mathbf{X}^{T}\mathbf{Z}\|_{2} - \|\mathbf{X}^{T}\mathbf{X}\|_{2}}{\|\mathbf{X}^{T}\mathbf{X}\|} \text{ respectively because}$ 

$$\frac{\left\|\mathbf{Z}^{\mathbf{T}}\mathbf{X}\right\|_{2}^{n} - \left\|\mathbf{Z}^{\mathbf{T}}\mathbf{Z}\right\|_{2}^{n}}{\left\|\mathbf{Z}^{\mathbf{T}}\mathbf{X}\right\|_{2} - \left\|\mathbf{Z}^{\mathbf{T}}\mathbf{Z}\right\|_{2}} = \frac{1 - \left(\frac{\left\|\mathbf{Z}^{\mathbf{T}}\mathbf{X}\right\|_{2}}{\left\|\mathbf{Z}^{\mathbf{T}}\mathbf{X}\right\|_{2}}\right)^{n}}{1 - \frac{\left\|\mathbf{Z}^{\mathbf{T}}\mathbf{X}\right\|_{2}}{\left\|\mathbf{Z}^{\mathbf{T}}\mathbf{Z}\right\|_{2}}} = \sum_{p=0}^{n-1} \left\|\mathbf{Z}^{\mathbf{T}}\mathbf{X}\right\|_{2}^{p} \left\|\mathbf{Z}^{\mathbf{T}}\mathbf{Z}\right\|_{2}^{p-1}$$

Therefore these fractional terms can be minimized by minimizing  $\|\mathbf{Z}^{T}\mathbf{X}\|_{2}$  and  $\|\mathbf{Z}^{T}\mathbf{Z}\|_{2}$  as the sums of products of decreasing functions of norms are also decreasing. By Cauchy-Schwarz inequality  $\|\mathbf{Z}^{T}(\mathbf{X} - \mathbf{Z})\| \leq \|\mathbf{Z}\| \|\mathbf{X} - \mathbf{Z}\|$ .

Therefore the upper-bound on difference of KL-divergence can be minimized by minimizing  $\|\mathbf{Z}\|$ and  $\|\mathbf{X} - \mathbf{Z}\|$  to minimize terms  $\|\mathbf{Z}^{T}\mathbf{X} - \mathbf{Z}^{T}\mathbf{Z}\|, \|\mathbf{X}^{T}\mathbf{Z} - \mathbf{X}^{T}\mathbf{X}\|$  in addition to minimizing  $\|\mathbf{Z}^{T}\mathbf{Z}\|, \|\mathbf{Z}^{T}\mathbf{X}\|_{2} = Tr(\mathbf{Z}^{T}\mathbf{X}\mathbf{X}^{T}\mathbf{Z}) = DCOV(\mathbf{X}, \mathbf{Z})$  to minimize terms  $\frac{\|\mathbf{Z}^{T}\mathbf{x}\|_{2}^{n} - \|\mathbf{Z}^{T}\mathbf{X}\|_{2}^{n}}{\|\mathbf{Z}^{T}\mathbf{X}\|_{2}^{n} - \|\mathbf{X}^{T}\mathbf{X}\|_{2}^{n}}, \frac{\|\mathbf{x}^{T}\mathbf{Z}\|_{2}^{n} - \|\mathbf{x}^{T}\mathbf{x}\|_{2}^{n}}{\|\mathbf{X}^{T}\mathbf{Z}\|_{2}^{n} - \|\mathbf{x}^{T}\mathbf{x}\|_{2}^{n}}.$  CVPR Tutorial On Distributed Private Machine Learning for Computer Vision: Federated Learning, Split Learning and Beyond

Distributed Private Machine Learning for Computer Vision: Federated Learning, Split Learning and Beyond Brendan McMahan, Jakub Konečný, Ramesh Raskar, Otkrist Gupta, Hassan Takabi, Praneeth Vepakomma

## Project Page and Papers: https://splitlearning.github.io/

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